Analysis of Co-evolving Gene Families Using Mutually Exclusive Orthologous Modules

Xiuwei Zhang*1, Martin Kupiec2, Uri Gophna2 and Tamir Tuller3,4*

1 Laboratory for Computational Biology and Bioinformatics, EPFL (Ecole Polytechnique Fédérale de Lausanne), Lausanne, Switzerland, and Swiss Institute of Bioinformatics. 2 Department of Molecular Microbiology and Biotechnology, Tel Aviv University, Ramat Aviv 69978, Israel.
3 Faculty of Mathematics and Computer Science, 4 Department of Molecular Genetics, Weizmann Institute of Science. Rehovot, Israel.
*XZ and TT contributed equally to this work.
Contact: tamirtul@post.tau.ac.il (TT)

Abstract: Co-evolutionary networks can encapsulate information about the dynamics of presence and absence of gene families in organisms. Analysis of such networks should reveal fundamental principles underlying the evolution of cellular systems and the functionality of sets of genes.

In this study, we describe a new approach for analyzing co-evolutionary networks. Our method detects Mutually Exclusive Orthologous Modules (MEOMs). A MEOM is composed of two sets of gene families, each including gene families that tend to appear in the same organisms, such that the two sets tend to mutually exclude each other (if one set appears in a certain organism the second set does not). Thus a MEOM reflects the evolutionary replacement of one set of genes by another due to reasons such as lineage/environmental specificity, incompatibility or functional redundancy.

We use our method to analyze a co-evolutionary network that is based on 383 microorganisms from the three domains of life. As we demonstrate, our method is useful for detecting meaningful evolutionary clades of organisms as well as sets of proteins that
interact with each other. Among our results, we report that:

1) MEOMs tend to include gene families whose cellular functions involve transport, energy production, metabolism, and translation, suggesting that changes in the metabolic environments that require adaptation to new sources of energy are central triggers of complex/pathway replacement in evolution. 2) Many MEOMs are related to outer membrane proteins; such proteins are involved in interaction with the environment and could thus be replaced as a result of adaptation. 3) MEOMs tend to separate organisms with large phylogenetic distance but they also separate organisms that live in different ecological niches. 4) Strikingly, although many MEOMs can be identified, there are much fewer cases where the two cliques in the MEOM completely mutually exclude each other, demonstrating the flexibility of protein evolution. 5) CO dehydrogenase and thymidylate synthase and the glycine cleavage genes mutually exclude each other in archaea; this may represent an alternative route for generation of methyl donors for thymidine synthesis.

1. Introduction

Co-evolution of genes is an important force constraining the evolution of genes, proteins and other cellular features and is useful for predicting physical and functional interactions [1, 2].

A natural way of representing co-evolutionary relations is by co-evolutionary networks [3-6]. In the case of co-evolution of genes, each node in a co-evolutionary network corresponds to a gene family (for example, a Cluster of Orthologous Groups of proteins (COG) [7]), and pairs of nodes are connected by an edge if they tend to appear in the same organisms. In some cases, the network can also encompass information about "anti-occurrence", i.e. proteins or cliques of proteins that tend not to appear in the same organisms are connected with a different type of edge [4].

Previous systems biology studies have mainly focused on other types of biological networks such as protein interaction networks (see, for example, [8, 9]), genetic interaction
networks [10, 11], and regulatory networks (e.g., [12, 13]) to understand cellular systems. One important difference between co-evolutionary networks and other biological networks is the fact that co-evolutionary networks encapsulate information about the evolutionary dynamics of cellular systems while the other networks provide a snapshot of a particular cellular system at a certain time point (i.e. in a specific organism). Thus, by analyzing co-evolutionary networks it should be possible to detect biological phenomena that cannot be detected by analyzing other biological networks.

In this study we describe a new computational approach for analyzing co-evolutionary networks. The aim of our method is to find Mutually Exclusive Orthologous Modules (MEOMs) - pairs of sets of gene families such that each set tends to appear in the same organisms, but the two sets usually do not co-occur (see Figure 1). These sets may describe cases of lineage specificity, where only one divergent lineage can benefit from a particular functional set. Another explanation can be incompatibility - cases where different cellular pathways cannot physically co-exist in the same organisms. Alternatively, they may simply represent functional streamlining where the loss of one cellular sub-function can be either due to redundancy, or an evolutionary consequence of different ecological constraints.

2. Results and Discussion

We analyze two co-evolutionary networks, one that corresponds to 95 organisms and was previously used [14] to reconstruct ancestral gene content and a new co-evolutionary network extracted from 383 microorganisms (see Methods); the smaller dataset is based on the commonly used COG database [7] and is a subset of the second dataset.

We performed the following general steps to obtain MEOMs: First, based on physical and statistical evidence we generated a co-evolutionary network of 383 organisms and 4870 COGs (Figure 1 A,B; Methods). In this network, we found MEOMs (two green cliques that are connected by a red bi-clique, i.e. a highly connected component of red edges; Figure 1 C-E; Methods) and analyzed the COGs and organisms corresponding to each MEOM. This procedure was implemented hierarchically: in each step we divided the set of
organisms to sub-taxonomical groups and applied our method to find MEOMs in each of these subsets separately (Figure 1 F).

**MEOMs divide the three domains of life according to ribosomal and proteasomal proteins**

To demonstrate our approach we began with a relatively small dataset (95 species of bacteria, archaea and eukaryotes). The most striking MEOM found by our method appears in Figure 2 (see Supplementary Table 1 for the list of all 9 MEOMs that were found for this dataset). One of the green cliques in this MEOM corresponded to a set of ribosomal proteins that appear exclusively in Bacteria while the second corresponded to the ribosomal proteins that only appear in Archaea (see Figure 2). Indeed, since bacterial and archaeal ribosomes differ significantly, many of the ribosomal proteins should appear either in Archaea or in Bacteria, they mutually excluding each other [15]. In addition, it was shown that the ribosomal proteins undergo less horizontal gene transfer (HGT) than other protein families [16]. In contrast, the only domain of life where both sets of ribosomal proteins appear is Eukarya – the archaeal ribosome is similar to the cytosolic eukaryotic ribosome while the bacterial ribosome is similar to the mitochondrial eukaryotic ribosome (see Figure 2). Reassuringly, this is exactly the result obtained in the ribosomal MEOM in Eukarya (Figure 2). Thus, although our method is unsupervised, and does not assume any phylogenetic tree, it accurately divided the organisms in the dataset into the three domains of life and identified the most central and evolutionarily conserved complex (the ribosome) that separates these organisms.

Another important complex that is specific to the archaeal/eukaryotic branch of the tree of life is the proteasome (the notable exception being *Mycobacterium tuberculosis* [17]). Indeed several proteasome subunits are also domain-specific MEOMs. Curiously, two proteins of unknown function, a GTPase and a putative transcription factor, appear as part of the eukaryotes/archaea-specific MEOM set. We can therefore speculate that it is highly likely that they represent some yet unidentified component of either the translational apparatus or proteasome-mediated degradation.
Analysis of a dataset of 383 species of bacteria, archaea and eukaryotes reveals the systems biological properties of MEOMs

To better obtain general evolutionary observations we extended our approach to analyze a larger dataset of 383 micro-organisms, better representing multiple levels of prokaryotic taxonomic diversity (see Figure 3A). In each sub-group of this dataset dozens of MEOMs were detected (the exact number of MEOMs that was detected in each sub-group appears in Figure 3A; the details about all the MEOMs found in each group of organisms appear in Supplementary Tables 2-8). We performed two randomization tests to show that the number of detected MEOMs is significant. In the first test, we compared the number of MEOMs to the result obtained for randomized co-evolutionary networks with a similar network degree distribution (see the Methods section). In the second test, we compared our MEOM data to the results obtained when we randomly assigned COGs to genomes while maintaining the same number of COGs in each genome (Methods and [5]). All the p-values but one were significant (i.e. all p-value < 0.0045); one p-value was borderline significant (p-value = 0.083); in most of the cases (all datasets for the first randomization, 5 out of 6 datasets for the second randomization) the number of detected MEOMs in the randomized networks was zero or close to zero (see details in Supplementary Tables 10). In addition, we performed Jackknifing (see, details in the Methods section) to show that most of the resultant MEOMs reported in the paper are robust to changes in the input database.

We found that 78% of the MEOMs appear in at least 90% of the sampled databases (96% of the MEOMs appear in at least 70% of the sampled databases) demonstrating that the results reported in the paper are robust, and that smaller datasets can also be used reliably (see details in supplementary table 10).

Flexibility in the co-evolution of protein complexes

Interestingly, excluding the eukaryotes, in all the other groups analyzed we found organisms that include both green cliques of the MEOMs (i.e. there are relatively few cases where these cliques completely mutually exclude each other, hinting to the existence of putatively incompatible gene families; Figure 3B). This is surprising as the aim of our algorithm is to find sets of orthologs with as few organisms with both cliques as possible.
This result demonstrates the great evolutionary flexibility of protein evolution, since it implies that almost any combination of two complexes can co-exist in the same cell without any deleterious effect, or at least that in some organisms an evolutionary solution can be found that allows this coexistence. This inherent flexibility and adaptability of cellular life could help explain why lateral gene transfer is such a common evolutionary phenomenon, since acquiring a functional complex in its entirety (for example by acquisition of a "selfish operon", [18]) will outweigh the possible deleterious effects, at least in some lineages. More generally, this result is in accordance with previous studies emphasizing the robustness and flexibility of many biological systems (see, for example, [19-23]).

**MEOMs tend to separate organisms with large phylogenetic distance but also separate organisms that live in different ecological niches**

In the next step we wanted to verify if MEOMs represent both evolutionary proximity and environmental changes. Thus, we performed the following experiment: we considered the dataset of all the bacteria; for each pair of bacterial species, we counted the number of times this pair of organisms appeared in different green cliques of a MEOM. We denote this number as the **MEOM separation index** of the pair of organisms.

We compared the MEOM separation of pairs of organisms with their evolutionary proximity (the topological distance in NCBI taxonomy; Methods) and their environmental proximity (according to [24], Methods). To show that the separation of MEOM decreases with phylogenetic distance while controlling for environmental proximity, we computed the correlation between the phylogenetic distance and the mean MEOM separations of organisms that do not inhabit the same environment (Spearman correlation \( r = 0.96; p = 2.4*10^{-10} \)) and for organisms that do live in the same niche (Spearman correlation \( r = 0.96; p = 3.3*10^{-9} \)). To show that MEOM separation decreases with environmental proximity we computed for each possible phylogenetic distance the mean MEOM separation of pairs of organisms with this phylogenetic distance. We computed such a vector of mean MEOM separation for pairs of organisms from the same community and pairs of organisms that are in different communities. We compared these vectors to show that a component in the first vector tends to be smaller than the corresponding component in the second vector; *i.e.* for every phylogenetic distance, pairs of organisms that are in the same community have lower
mean MEOM separation indexed than pairs of organisms that are in different communities (Wilcoxon test: $p = 0.0005$). The corresponding graphs appear in Figure 3 C-E, and show that the mean MEOM separation increases both with the mean evolutionary distance (even when controlling for environmental distance) and with environmental distance [24] (even when controlling for evolutionary distance). In addition we performed a multivariate regression analysis (see details in the Methods section). We showed that 1) there is correlation between MEOM separation and phylogenetic proximity even when controlling for ecological proximity and the size of the genomes together. 2) There is a correlation between MEOM separation and ecological proximity even when controlling for phylogenetic proximity and the size of the genomes together ($p < 10^{-16}$ in both cases). These results suggest that MEOMs reflect both lineage specific and adaptation-driven changes (e.g. due to a shift in environmental conditions or lateral gene transfer).

**MEOMs are enriched with metabolic genes and outer membrane proteins**

In order to understand if there are cellular functions that tend to appear more frequently in MEOMs, we computed for each group of organisms the number of times each cellular function appears in a MEOM. We considered three functional ontologies: the GO ontology of *S. cerevisiae* [25], the GO ontology of *E. coli* [25], and the more general COG ontology [7]. Table 1 depicts the top cellular functions that are enriched in MEOMs when considering the COG ontology. As can be seen, the main cellular functions that are enriched in MEOMs relate to 'Transport', 'Energy production', 'Metabolism', and 'Translation' (similar results were obtained when we used the GO ontologies of *E. coli* or *S. cerevisiae*; Supplementary Table 9; all the p-values appear in Supplementary Table 1-8) suggesting that changes in the metabolic environments that require adaptation to new sources of energy are central triggers of complex/pathway replacement in evolution.

In addition, we see many results that are related to outer membrane proteins (for example, 5 out of the 21 bacterial MEOMs were enriched with GO terms related to the outer membrane). Such proteins are involved in the interaction of Gram-negative bacteria with the environment and could thus be replaced as a result of adaptation (indeed, when considering only these MEOMs, for every phylogenetic distance, pairs of organisms that
are in the same community have lower mean MEOM separation than pairs of organisms that are in different communities; Wilcoxon test: p = 0.005). Furthermore, different organismal lineages differ in their cellular envelope structure, imposing different constraints on the families of outer membrane proteins that can be found in them (e.g. lipid monolayers in some archaea, double membranes in Gram-negative bacterial lineages, mycolic acid in some cell walls, etc). Thus for example, in Bacteria (bacterial MEOM 1) the Gram-positive bacteria that do not possess the conserved outer membrane proteins common to Gram-negatives, have a mutually-exclusive clique of protein components of a putative ABC transporter, which includes a typical Gram positive lipoprotein substrate-binding subunit.

Our algorithm detects pairs of cliques, each with very strong co-evolutionary relations. Therefore in many cases, the entire clique is replaced by another clique. Thus, the algorithm identifies only very rigid co-occurrence cliques, i.e. protein complexes (or sub-complexes) where subunits cannot be substituted by members of other protein families while still maintaining the function of the complex. This often results in the identification of the most basic functional modules within a complex. Our results imply that acquisition and subsequent replacement of subunits in these complexes (or sub-complexes) by lateral gene transfer will only proceed through xenologous gene replacement, rather than by introduction of non-homologous subunits. Thus, it is possible that many of the cliques reported in this paper (e.g., the outer membrane complexes and ribosomal/proteosomal sub-complexes mentioned above) are such basic functional modules.

**Mutually exclusion of H+-ATPase and F-ATPase in bacteria and archaea**

We described above an example of mutually exclusive complexes due to divergence of lineages, i.e. the translational apparatus of Archaea and Bacteria. In the case of the ribosome lineage divergence probably coincides with incompatibility, since the same cell cannot harbor two different ribosome types, unless some compartmentalization had occurred (e.g. eukaryotic organelles). However, mutually exclusive protein complexes can also be a result of the loss of functional redundant complexes, where an activity does not need to be carried out by two parallel mechanisms. This situation can arise following
acquisition of a gene cluster by HGT or after a large duplication event. An interesting example is the case of the Archaeal/vacuolar-type H+-ATPase in bacteria [26-28]. Bacteria in general lack the Archaeal/vacuolar-type H+-ATPase complex, with a few notable exceptions attributed to lateral gene transfer, such as the spirochete Borrelia burgdoferi [27, 29] and Chlamydia species [30], both intracellular pathogens. Curiously these intracellular bacteria have lost the ancestral bacterial F-ATPase, hence their detection as MEOMs (when considering the entire dataset; see Figure 4), and it appears likely that the laterally acquired ATPase now pumps out protons from the cytoplasm and generates a proton gradient, for energy, transport, or both, similar to the role of the ancestral bacterial system [31]. One can speculate that the reason that the acquired ATPase replaced the ancestral one is some adaptation to life inside a eukaryotic cell.

**Mutual exclusion of CO dehydrogenase/thymidylate synthase and the glycine cleavage genes—clues for thymidine metabolism in archaea?**

While proteins of the putative glycine cleavage system are abundant in archaea, their roles are unclear and a Haloferax volcanii mutant defective for one of its components, dihydrolipoamide dehydrogenase, showed no growth inhibition on a variety of minimal media [36]. These genes are present in all archaea in our dataset, except the methanogens and Archaeoglobus fulgidus, an archeon that also has some methanogenesis-related genes. The latter organisms have a clique of proteins mutually exclusive with the glycine cleavage system. These proteins include CO dehydrogenase, which is found in methanogenic archaea, and can function either as an acetyl-CoA synthase or in the fermentation of acetate to methane [35]. Another protein in this clique is the ThyA type thymidylate synthase. Since methanogens do not synthesize folate and its derivatives, it is assumed that different molecules provide the required methyl group for converting dUMP to dTMP, such as the modified folate tetrahydromethanopterin. Glycine can provide a methylene group by glycine cleavage and generate either 5,10-methylenetetrahydrofolate (from tetrahydrofolate), or the analogous tetrahydromethanopterin. Thus archaeal species that have the alternative thymidylate synthase ThyX [41] may use glycine cleavage for dTMP synthesis. We therefore predict that unlike the lack of phenotype observed in the Hfx. volcanii mutant, [36] the same mutation in the halophilic archeon Halobacterium
salinarum, which relies on ThyX rather than ThyA [32], should yield a strain deficient in the synthesis of thymidine.

3. Conclusion

Co-evolutionary networks represent relations between proteins that tend to co-evolve. These networks can yield important evolutionary insights at the individual complex level as well as reveal important general trends in evolutionary systems biology, yet few methods to explore these networks have been developed. Here we used a novel approach for analyzing co-evolutionary networks. Our method captures both lineage-specific and environment-specific changes, and can therefore be used independently of an organismal phylogeny, to investigate complex evolutionary scenarios that include horizontal gene transfer, gene duplication and lineage-specific changes in very large number of organisms. This is important, since most evolutionary algorithms rely on a given "tree of life", whereas in reality many relationships are not well supported due to horizontal gene transfer [33, 34], or simply because deep relationships no longer maintain sufficient evolutionary signal [35]. Another important feature of our method is that it was designed to infer both relations between organisms and between gene families. Thus, it adds an additional dimension to previous approaches in molecular evolution that mainly infer either relations between gene families (see, for example, [4, 14, 36]) or between organisms (see, for example, [3, 33, 37]). Another advantage of our approach is the fact that it can be implemented in a hierarchical manner to study biologically relevant groups of organisms, at different taxonomic levels, revealing key adaptations of subsets within phylogenetic groups.

The fact that most of the cliques reported in this paper corresponded to known functional complexes confirms that our method usually detects biologically meaningful results. In addition, it suggests that it can be applied in the future for detecting functional relations between gene families. A gene family that is connected by co-evolutionary relations to many gene families with a certain function probably has a similar cellular function (see also [4]). For example, MEOM 8 of the Actinobacteria includes many flagellar genes but also some uncharacterized proteins. We believe that the uncharacterized proteins may also be related to motility (other examples were reported above). The MEOM principle can also be
generalized to study different network types. Thus, one can analyze networks whose nodes correspond to domains within proteins or organisms in a community network [24].

4. Methods

**Information about Taxonomy:** This information was downloaded from ftp://ftp.ncbi.nih.gov/pub/taxonomy/

**Obtaining the input network:**

The nodes in the analyzed networks correspond to the 4870 COGs [7] in a large dataset of organisms that will be discussed later.

The co-evolutionary networks used in this study were based on two sources of information: 1) Evidence of co-functionality or physical interactions (e.g. the String databases mentioned below). 2) Statistical evidences related to co-occurrence of pairs of COG in the analyzed genomes.

We put edges between pairs of COGs only if they satisfy these two conditions. This is a generic and "modular" approach: i.e. it is possible to replace the first source of information with a different one. It is also possible to use only the second source of information. Similar ideas were used in [14] with very good results.

Specifically, the co-evolutionary edges were based on information downloaded from the String database [38]. This database includes information on genomic neighborhood, co-expression, gene fusion and more. Each co-evolutionary relation in this dataset was based on a composite score, which is a weighted average of these sources of information. The initial number of co-evolutionary relations downloaded from this database was 962,618.

For a co-evolutionary edge to be included in the network it should also satisfy additional statistical requirements:

Let \( pr00 \) denote the empirical probability that a pair of orthologs does not appear in the same organism; let \( pr01 \) denote the probability that the first ortholog does not appear while the second does; let \( pr10 \) denote the probability that the first ortholog appears while the second does not appear; finally, let \( Pr11 \) denote the probability that the two orthologs
appear in the same organism. Let “green” denote a positive co-occurrence relation between the two orthologs, and “red” denote a negative co-occurrence relation. We considered only significant edges that exhibit

(A) a strong co-evolutionary relation, and

(B) the pattern of occurrence/absence of the pair of proteins is variable: In the case of green edges, there are organisms with both proteins but also organisms with neither. In the case of red edges, there are genomes encoding one of the proteins but not the other, but there are also cases in which the presence/absence pattern of these proteins is the opposite (the second protein is encoded in the genome but the first one is not).

Statistically, pairs of orthologs with stronger condition (B) are more surprising as they correspond to cases where there have been more evolutionary changes in the presence/absence pattern of each of the proteins/orthologs but the changes of the two proteins were correlated.

Specifically, we considered the following conditions ($k_1$ and $k_2$ are two thresholds):

To satisfy condition A:

1. Candidates for green edges: calculate $g_1 = (pr_{00} + pr_{11})/(pr_{01} + pr_{10})$ for each edge, and choose the first $(1-k_1)*962618$ edges which have the highest $g_1$ value.

2. Candidates for red edges: calculate $r_1 = (pr_{01} + pr_{10})/(pr_{00} + pr_{11})$ for each edge, and choose the first $(1-k_1)*962618$ edges which have the highest $r_1$ value (these edges also have the lowest $g_1$ value).

To satisfy condition B:

3. For each potentially green edge calculate an additional value: $g_2 = max(pr_{00}, pr_{11}) / min(pr_{00}, pr_{11})$; choose only the edges that have $g_2<k_2$ to be green.

4. For each potentially red edge calculate an additional value: $r_2 = max(pr_{01}, pr_{10}) / min(pr_{01}, pr_{10})$; choose only the edges who have $r_2<k_2$ to be red.

The small network

This graph corresponds to a set of 95 bacteria, archaea, and eukaryotes downloaded from [14]. By letting $k_1 = 95\%$ and $k_2 = 10$, we obtain a network with 24,944 edges and 2,421 different orthologs. Specifically, it includes 5,242 red edges and 19,702 green edges.
The large network

This graph corresponds to the gene content of 383 bacteria and archaea, and eukaryotes. These data were downloaded from NCBI (ftp://ftp.ncbi.nih.gov/genomes/) and based on the dataset from [39]; the data were analyzed hierarchically. The hierarchical partitioning of the data was based on NCBI taxonomy (ftp://ftp.ncbi.nih.gov/pub/taxonomy/>.

At the first stage, we analyzed the entire dataset by letting $k_1 = 90\%$ and $k_2 = 10$, we obtain a network with 31,451 edges and 2,324 different orthologs. Specifically, it includes 3,655 red edges and 27,796 green edges.

At the next stage we analyzed eukaryotes (18 organisms; 68,527 green edges, 1,444 red edges, and 1,095 COGS), archaea (27 organisms; 672 green edges, 1,456 red edges, 1,047 COG), and bacteria (340 organisms; 15,836 green edges and 1,083 red edges, 1,855 COGs) separately.

At the next stage, we analyzed a few large bacterial sub-groups (groups with more than 20 organisms):

- Proteobacteria (199 organisms; 8,962 green edges, 490 red edges, and 1,405 COGs),
- Firmicutes (59 organisms; 28,021 green, 522 red edges, and 1,235 COGs),
- Actinobacteria (26 organisms; 6,923 green, 490 red edges, and 1,127 COGs; we used here $k_1=0.85$).

Scoring MEOMs

We used an algorithm that is based on [11]. The optimization score was based on [10]. Let $G^+(V, E^+)$ be the network induced when considering only the positive co-evolutionary relations (the green edges); let $G^-(V, E^-)$ be the network induced when considering only the reciprocal co-evolutionary relations (the red edges). The nodes, $V$, in these networks are the set of genes families (COGs). A MEOM is a pair of disjoint sets $V_1, V_2$, such that

(a) $|V_2|, |V_1| \geq 2$; (b) For each $V_i$, there are unusually many green edges between $V_i$; and (c) there are unusually many red edges between $V_1$ and $V_2$ (see Figure 1).
To quantify property (b), we derive a log-odds score reflecting the likelihood that the
density of green edges between nodes in $V_1$ or in $V_2$ is unusually high. We compare two
hypotheses: under the MEOM hypothesis, every pair of genes, one from $V_i$ ($i=1$, or $i=2$),
has a co-evolutionary relation (green edges) with a high probability $\alpha$, independently of all
other gene pairs, and the likelihood of a model $V_i$ is

$$\prod_{(a,b)\in[V_i\times V_i]} \alpha \cdot I(a,b) + (1-\alpha) \cdot (1-I(a,b)),$$

where $I(a,b)$ equals 1 if there exists a red edge

between $a$ and $b$ and otherwise it equals 0; in the null hypothesis, every pair $(a, b)$ is
connected with probability $r(a,b)$, representing the chance of observing this interaction at
random, given the degrees of $a$ and $b$ in $G$.$^g$. We estimate $r(a,b)$ by generating a random
ensemble of networks with the same degree sequence and counting what fraction of them
contain an interaction between $a$ and $b$. The log-odds score is then

$$S^g(V_i) = \log \left( \frac{\prod_{(a,b)\in[V_i\times V_i]} \alpha \cdot I(a,b) + (1-\alpha) \cdot (1-I(a,b))}{\prod_{(a,b)\in[V_i\times V_i]} r(a,b) \cdot I(a,b) + (1-r(a,b)) \cdot (1-I(a,b))} \right).$$

Similarly, to quantify property (c) we derive a log-odds score reflecting the likelihood that
the density of red edges between $V_1$ and $V_2$ is unusually high. We compare two hypotheses:
under the MEOM hypothesis, every pair of genes, one from $V_1$ and the other from $V_2$, have
reciprocal co-evolutionary relation (red edges) with a high probability $\beta$, independently of all
other gene pairs, and the likelihood of a model $(V_1, V_2)$ is thus

$$\prod_{(a,b)\in[V_1\times V_2]} \beta \cdot I(a,b) + (1-\beta) \cdot (1-I(a,b)),$$

where $I(a,b)$ equals 1 if there exists a red edge

between $a$ and $b$ and otherwise it equals 0; in the null hypothesis, every pair $(a, b)$ is
connected with probability $r(a,b)$, representing the chance of observing this interaction at
random, given the degrees of $a$ and $b$ in $G'$. We estimate $r(a,b)$ by generating a random
ensemble of networks with the same degree sequence and counting what fraction of them
contain an interaction between \( a \) and \( b \). The log-odds score is then

\[
S'(V_1, V_2) = \log \left( \frac{\prod_{(a,b)\in (V_1 \times V_2)} \beta \cdot I(a,b) + (1-\beta) \cdot (1-I(a,b))}{\prod_{(a,b)\in (V_1 \times V_2)} r(a,b) \cdot I(a,b) + (1-r(a,b)) \cdot (1-I(a,b))} \right).
\]

The final score was \( S'(V_1, V_2) + S^g(V_1) + S^g(V_2) \). The aim was to find sub-networks whose score is as large as possible. We filtered sub-networks whose probability in randomized networks with similar degree distribution (see below how these networks were computed) was \( > 0.05 \). To assess the statistical significance of the results we performed the two randomization tests described below:

**Two network randomization tests**

In this paper we report two randomization tests.

In the first randomization test we generated for each dataset a random ensemble of networks (a total of 20 networks) with the same degree distribution of red and green edges (see, for example, [4]). We counted what fraction of them contained more MEOMs than the original network.

The second randomization test was similar to the one reported in [5]. In this randomization test we generated a total of 20 networks where we randomly assigned COGs to each organism maintaining the total number of COGs in the organism. In this case we used \( k \) such that the number of edges in the random network will be similar to the number of edges in the original network.

**Jackknifing**

Jackknifing (see, e.g., [40]) was performed as described below.

Repeat 100 times:
1. Randomly choose 90\% of the edges in the network (STRING).
2. Run the algorithm to find MEOMs.

Count for each MEOM the number of times it appears (Jaccard index [41] \( > 0.5 \) corresponding to the nodes in the two MEOMs) in resultant random networks.
**MEOMs' separation vs. phylogenetic/environmental proximity**

To show that the separation of MEOMs corresponds both to phylogenetical proximity and to environmental proximity we used the following definitions:

A pair of organisms is separated by a MEOM if one of them has most of the COGs (*i.e.* more than 50%) of the first cluster but does not have most of the genes (COGs) of the second cluster while the second organism have most of the genes of the second cluster but does not have most of the genes of the first cluster. The MEOMs' separation score for a pair of organisms is the number of times these two organisms are separated by a MEOM.

Evolutionary proximity between two organisms was defined as the number of nodes separating the two taxa in NCBI-taxonomy tree (see, for example, [42]).

A pair of organisms was defined to share environments if it appears in the same community according to [24].

To control for the size of the genomes of the analyzed organisms we computed for each pair of genomes the mean number of COGs in that pair. We performed non-parametric multivariate analysis (see details below) where we computed the following correlations 1) correlation between MEOM separation and *phylogenetic* proximity when controlling for *ecological* proximity and the size of the genomes together. 2) correlation between MEOM separation and *ecological* proximity when controlling for *phylogenetic* proximity and the size of the genomes together. The correlations were 0.53 and -0.082 respectively (p < 10^{-16} in both cases).

**Non-parametric multivariate analysis:** Let X, and Y denote two variables and Z=[Z1, Z2, Z3,..] denote a set of variables. The non-parametric multivariate analysis that is reported in this paper includes partial Spearman correlations of the form R(X,Y|Z). Roughly, if such a correlation is significant it means that there is a relation between X and Y that cannot be explained by the variables in Z.

**Acknowledgments**
We would like to thank Dr. Igor Ulitsky, Prof. Elchanan Mossel, and Prof. Yitzhak Pilpel for very helpful discussions. T.T. is a Koshland Scholar at Weizmann Institute of Science. MK’s research was supported by grants from the Israel Science Foundation and the McDonnell Foundation. UG is supported by the McDonnell Foundation and the Israeli Ministry of Health.

Supplementary Files

The supplementary files appear in the .zip file

Figures
Figure 1. Finding MEOMs in co-evolutionary networks: a flow diagram. A. A co-evolutionary network is reconstructed based on biological (e.g. physical interaction, co-expression, etc.) and statistical evidence. B. In a co-evolutionary network each node corresponds to a gene family; green edges denote co-occurrence of the two nodes in the same organisms; red edges denote mutually exclusive occurrence (i.e., occurrence in different organisms). C. The optimization score of a MEOM was based on [10]. D. Each MEOM is composed of two green (close to) cliques that are connected by a red (close to) bi-clique; in practice, the green (red) cliques (bi-cliques) may not be perfect (i.e. some of the edges may be missing; Methods). E. Projection of a MEOM on a (gene family)*(organism) table; black denotes a case where there is a gene from the gene family in the organism; white denote cases where no gene from the gene family appears in the organism. F. The approach can be implemented iteratively on sub-taxonomic / phylogenetic groups.
Figure 2. The most striking MEOM detected in dataset of 95 organisms. A. The co-evolutionary edges between the gene families that are part of the MEOM. B. The solution splits the analyzed organisms to the three domains of life (Bacteria, Archaea and Eukarya).

Figure 3. General properties of MEOMs. A. The sub-groups that were analyzed from a dataset of 383 organisms, the number of organisms in each sub-group (blue) and the number of MEOMs that were detected in each sub-group (red). B. Number of incomplete mutually exclusions in each of the analyzed group of organisms (out of the total number of MEOMs detected). C.-E. MEOMs reflect both lineage specificity and environmental changes. C. Mean MEOMs' separation increases with phylogenetic distance (Methods) for pair of organisms that are not in the same environment (Spearman correlation $r = 0.96; p = 2.4 \times 10^{-10}$). D. Mean MEOM separation increases with phylogenetic distance for pair of organisms that are in the same environment (Spearman correlation $r = 0.96; p = 3.3 \times 10^{-9}$). E. For every phylogenetic distance, pairs of organisms that are in the same community (Method) have lower mean MEOM separation than pairs of organisms that are in different communities (Wilcoxon test: $p = 0.0005$).
Figure 4. One of the MEOMs found in the entire dataset (383 organisms): the 'Archaeal/vacuolar-type H+-ATPase' vs. 'F0/F1-type ATP synthase'. The COGs related to these two pathways are marked.

<table>
<thead>
<tr>
<th>Group of Organisms</th>
<th>Cellular Functions</th>
<th>Number of MEOMs with the function</th>
<th>Total number of enriched functions</th>
<th>total number of MEOMs</th>
<th>Most/least significant p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>All</td>
<td>Translation, ribosomal structure and biogenesis</td>
<td>4</td>
<td>16</td>
<td>22</td>
<td>2.22e-16/2.27e-02</td>
</tr>
<tr>
<td>Domain</td>
<td>Functional Category</td>
<td>Version</td>
<td>Release</td>
<td>Offset</td>
<td>E-values</td>
</tr>
<tr>
<td>-------------</td>
<td>----------------------------------------</td>
<td>---------</td>
<td>---------</td>
<td>--------</td>
<td>----------</td>
</tr>
<tr>
<td><strong>Archaea</strong></td>
<td>Energy production and conversion</td>
<td>1</td>
<td>11</td>
<td>22</td>
<td>4.46e-11/6.88e-04</td>
</tr>
<tr>
<td></td>
<td>Amino acid transport and metabolism</td>
<td>1</td>
<td>11</td>
<td>2</td>
<td>4.43E-004</td>
</tr>
<tr>
<td><strong>Bacteria</strong></td>
<td>Energy production and conversion</td>
<td>5</td>
<td>14</td>
<td>21</td>
<td>6.08e-12/4.88e-04</td>
</tr>
<tr>
<td></td>
<td>Replication, recombination and repair</td>
<td>2</td>
<td>14</td>
<td>21</td>
<td>1.19e-05/1.06e-3</td>
</tr>
<tr>
<td><strong>Eukaryotes</strong></td>
<td>Translation, ribosomal structure and biogenesis</td>
<td>1</td>
<td>4</td>
<td>14</td>
<td>2.21E-008</td>
</tr>
<tr>
<td></td>
<td>Amino acid transport and metabolism</td>
<td>1</td>
<td>4</td>
<td>14</td>
<td>2.21E-008</td>
</tr>
<tr>
<td><strong>Proteobacteria</strong></td>
<td>Energy production and conversion</td>
<td>5</td>
<td>10</td>
<td>9</td>
<td>2.41e-13/7.58e-04</td>
</tr>
<tr>
<td></td>
<td>Carbohydrate transport and metabolism</td>
<td>3</td>
<td>10</td>
<td>9</td>
<td>6.88e-10/4.45e-05</td>
</tr>
<tr>
<td><strong>Firmicutes</strong></td>
<td>Energy production and conversion</td>
<td>2</td>
<td>3</td>
<td>5</td>
<td>4.07e-05/5.16e-04</td>
</tr>
</tbody>
</table>
Table 1. Cellular functions (COG ontology; [7]) that tend to appear in MEOMs. We considered only the top two cellular functions in each group; all the results (enriched cellular functions and the corresponding p-values and two additional functional annotations of genes) appear in the Supplementary Tables 1-9 (specifically, Supplementary Table 9 includes a summary of the results).

References


